Application of MATLAB environment to solution of boundary and initial boundary value problems

Partial Differential Equation Toolbox (PDETOOL)

PDETOOL is a GUI application that computes Finite Element Method approximation of solutions to partial differential equations (including eigen problems) in 2D spatial domains and time.

Selected problems:

- I. Plane strain state, static analysis
- II. Modal analysis (eigen vibrations)

Modeling process:

1. Type command *pdetool* in MATLAB Command Window without arguments to start the application.



Fig. 1: GUI of PDE Toolbox

2. Select the analyzed problem (Structural Mechanics, Plane Strain) toggling down the list with *Generic Scalar* option set as the default PDE type.

3. Specify your problem parameters by clicking the *PDE* icon in the main toolbar or select $PDE \rightarrow PDE$ Specification in the main menu and select either

- I. Elliptic problem or
- II. Eigen modes

and enter E - Young modulus, nu - Poisson ratio, Kx, Ky - components of body forces, rho - density.

4. Geometry definition

Set the limits of the coordinate system (*Options* \rightarrow *Axes Limits*) and turn on the grid (*Options* \rightarrow *Grid*). In order to define the geometry of the analyzed domain, use main toolbar icons (or *Draw* \rightarrow ... from the main menu).

Created geometrical figures are automatically named. One can modify a figure and its name clicking twice within the object. *Snap to grid* function may be turned on/off in *Options* menu in order to align objects to the grid.

Defined objects are summed up by default (e.g. R1+P1 denotes union of two figures). The default formula can be easily modified at the *Set formula* line. In order to delete an object, select it by a single click (its boundary is marked black then) and press *Delete* key.

5. Boundary condition types:

- Dirichlet b.c. (respective edges are marked with red color),
- Neumann b.c. (blue color)
- mixed (black color).

Homogeneous Dirichlet b.c. are set for each edge by default. To modify it, use the respective icon from the main toolbar or select *Boundary* \rightarrow *Specify Boundary Conditions* from the main menu. One can just click twice the respective edge and the same dialog box should pop out. Select multiple edges with *Shift* key pressed. Subsequently specify carefully respective boundary conditions.

			Boundary condition equation:			
Condition type: Coeffic	cient Value		Description			
Neumann g1	0		Surface tractions			
Dirichlet g2	0					
Mixed q11, q	12 0	0	Spring constants			
q21, q	122 0	0				
h11, h	12 1	0	Weights			
h21, h	122 0	1				
r1	0.01		Displacements			

Fig. 2: Non-zero Dirichlet b.c. definition

6. Mesh generation

Use one of two icons from the main toolbar in order to create either a coarse or fine mesh. The same can be done using main menu ($Mesh \rightarrow Initialize Mesh/Refine Mesh$).

7. Solving the problem

Click the '=' button or select *Solve* \rightarrow *Solve PDE* from the main menu. Solution plots will be presented.

II. Upper and lower bounds of the eigen values that are to be found can be specified in the main menu (*Solve* \rightarrow *Parameters*).

8. Postprocessing (visualization)

Select the respective icon in the main toolbar or select $Plot \rightarrow Parameters$ from the main menu in order to select solution maps, contour plot, deformed mesh, FE mesh options. *Colormap hsv* is recommended.

II. Mode shapes for selected range of eigen values can be plotted using *Eigenvalues* option.

All the data can be exported to the MATLAB Workspace in a matrix form. In particular, option $Mesh \rightarrow Export$ enables saving the information about the topology (p– node coordinates, e– edges, t – triangles), option $PDE \rightarrow Export$ saves the equation coefficients, option $Solve \rightarrow Export$ saves the solution values.

I. After exporting the necessary information (topology + equation coefficients and solution values) one can compute components of the strain and stress tensor and the Mises equivalent stress using intrinsic MATLAB procedure pdesmech, e.g.: sx=pdesmech(p,t,c,u,'tensor','sxx') mises=pdesmech(p,t,c,u,'tensor','von Mises','application','pn','nu',0.3)

The prepared model data can be saved as an M-file and modified using MATLAB Editor. After running such a file, GUI is opened automatically.