

$$p(x) = \sum_{j=1}^m a_j \varphi_j(x) \quad \left\{ \begin{array}{l} A_{i,j} a_j = B_i, \quad A_{i,j} = (\varphi_i, \varphi_j), \quad B_i = (f, \varphi_i) \quad - \text{przypadek ciągły} \\ \mathbf{C} \mathbf{a} = \mathbf{D}, \quad \mathbf{C} = \mathbf{A}^T \mathbf{A}, \quad \mathbf{D} = \mathbf{A}^T \mathbf{B}, \quad A_{i,j} = \varphi_j(x_i), \quad B_i = f(x_i) \quad - \text{przypadek dyskretny} \end{array} \right.$$

$$T_m(x) = \left\{ \begin{array}{l} T_1(x) = 1 \\ T_2(x) = x \\ T_m(x) = 2 \cdot x \cdot T_{m-1}(x) - T_{m-2}(x) \end{array} \right. \quad \left\{ \begin{array}{l} x_i = \cos \left(\frac{2 \cdot i - 1}{m-1} \cdot \frac{\pi}{2} \right), \quad i = 1, 2, \dots, m-1 \\ x \rightarrow z : z = \frac{1}{2}[(b-a)x + (b+a)] \end{array} \right.$$

$$(\varphi_i, \varphi_j) = \int_a^b \varphi_i \varphi_j dx, \quad (\varphi_i, \varphi_j, \mu) = \int_a^b \varphi_i \varphi_j \mu dx$$

$$\text{Ortogonalność: } (\varphi_i, \varphi_j) \left\{ \begin{array}{l} = 0, \quad i \neq j \\ \neq 0, \quad i = j \end{array} \right. \quad \text{Ortonormalność: } (\varphi_i, \varphi_j) \left\{ \begin{array}{l} = 0, \quad i \neq j \\ = 1, \quad i = j \end{array} \right.$$

$$\left(T_i, T_j \frac{1}{\sqrt{1-x^2}} \right) \left\{ \begin{array}{l} 0, \quad i \neq j \\ \frac{\pi}{2}, \quad i = j \neq 0 \\ \pi, \quad i = j = 0 \end{array} \right.$$

$$s(x) = p(x) + \sum_{i=2}^{n-1} b_i (x-x_i)_+^k = \sum_{i=1}^{k+1} a_i x^{k+1-i} + \sum_{i=2}^{n-1} b_i (x-x_i)_+^k, \quad (x-x_i)_+^k = \left\{ \begin{array}{ll} (x-x_i)^k, & \text{dla } x > x_i \\ 0, & \text{dla } x \leq x_i \end{array} \right.$$

$$b_j = \frac{f_{j+1} - p(x_{j+1}) - \sum_{i=2}^{j-1} b_i (x_{j+1} - x_i)^k}{(x_{j+1} - x_j)^k}, \quad j = 2, 3, \dots, n-1$$

$$\alpha \cdot u_{xx} - u_t = f, \quad (x, t) \in \Omega, \quad a \leq x \leq b, \quad t \geq t_0$$

$$\left\{ \begin{array}{l} u_{i,k+1} = \lambda u_{i-1,k} + (1-2\lambda)u_{i,k} + \lambda u_{i+1,k} - \Delta t \cdot f_{i,k}, \quad \lambda = \frac{\alpha \Delta t}{h^2}, \quad \lambda < 0.5 \\ u_{i,k} = -\lambda u_{i-1,k+1} + (1+2\lambda)u_{i,k+1} - \lambda u_{i+1,k+1} + \Delta t \cdot f_{i,k+1} \end{array} \right.$$

$$u_{xx} - \beta u_{tt} = f, \quad (x, t) \in \Omega, \quad a \leq x \leq b, \quad t \geq t_0$$

$$u_{i,k+1} = \lambda u_{i-1,k} + u_{i,k}(2-2\lambda) + \lambda u_{i+1,k} - u_{i,k-1} - \frac{\Delta t^2}{\beta} f_{i,k}, \quad \lambda = \frac{\Delta t^2}{\beta h^2}, \quad \lambda < 1$$

$$E(X) = \sum_{i=1}^k x_i p_i, \quad E(X) = \int_{-\infty}^{+\infty} x f(x) dx$$

$$V(X) = \sum_{i=1}^k (x_i - E(X))^2 p_i, \quad V(X) = \sigma^2 = \int_{-\infty}^{+\infty} (x - E(X))^2 f(x) dx$$

$$D^2(X) = \left(\sum x_i^2 p_i \right) - \left(\sum x_i p_i \right)^2$$

$$D^2(X) = \int_{-\infty}^{+\infty} x^2 f(x) dx - \left(\int_{-\infty}^{+\infty} x f(x) dx \right)^2$$

$$F(x) = P(X \leq x) = \sum_{x_i \leq x} P(X = x_i) = \sum_{x_i \leq x} p_i, \quad F(x) \equiv P(X \leq x) = \int_{-\infty}^x f(u) du$$

$$\lim_{\Delta x \rightarrow 0^+} \frac{P(x \leq X < x + \Delta x)}{\Delta x} = \lim_{x \rightarrow 0} \frac{F(x + \Delta x) - F(x)}{\Delta x} = F'(x).$$